

Chapter  
8



RRSP

RESP  
Mutual Funds

*Financial  
Mathematics:  
Investing  
Money*

Stocks  
Bonds

## 8.5 Investments Involving Regular Payments

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From grade 10...

**Principal:** the original amount invested or borrowed

**Interest rate:** the percentage charged, usually stated as a per year rate

**Simple interest:** interest calculated as a percentage of the principal

**Term:** the time in years for an investment or loan

**Compound interest:** the interest paid on the principal plus interest

**Compounding period:** the time between calculation of interest, also called the interest period

To calculate simple interest  $I = Prt$ .

P = the principal      r = rate of interest      t = term of the investment

To calculate the value of investment with compound interest over a long term students will use the following formula:

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

P = the principle      r = annual interest rate

n = number of compounding periods in a year

t = term of the investment or loan in years

Example 1:

$$1.75\% = 0.0175$$

Gordon wants to invest \$2000.00. His bank offers an investment option that earns simple interest at a rate of 1.75% per year.

- If he invests the money for 1 year, how much interest will Gordon earn?
- If he invests the money for 2 years, how much interest will Gordon earn?
- Based on your answers above, write an equation that can be used to calculate simple interest.

$$\frac{1.75}{100} = 0.0175$$

$$\begin{aligned} (a) \quad & 2000 \times 1.75\% \\ &= 2000 \times 0.0175 (1) \\ &= 35 \end{aligned}$$

$$\begin{aligned} (b) \quad & 2000 \times 1.75\% \times 2 \\ &= 2000 \times 0.0175 \times (2) \\ &= 70 \end{aligned}$$

$$(c) \quad I = P \times r \times t$$

$\downarrow$  amount of Interest       $\leftarrow$  Rate of Interest       $\leftarrow$  term in years

$\leftarrow$  Principle

You Try:

Becky wants to invest \$1000. Her bank offers an investment option that earns simple interest at a rate of 1.25% per year.

How much will she have at the end of the year?

$$I = Prt$$

$$I = (\$1000)(1.25\%)(1)$$

$$I = (\$1000)(0.0125)(1)$$

$$I = \$12.50$$

$$\$12.50 + \$1000 = \$1012.50$$

How much will she earn at the end of 2? 5 years?

$$I = Prt$$

$$I = (\$1000)(1.25\%)(2)$$

$$I = \$25$$

$$\$25 + \$1000 = \$1025$$

$$I = Prt$$

$$I = (\$1000)(1.25\%)(5)$$

$$I = \$62.50$$

$$\$62.50 + \$1000$$

$$= \$1062.50$$

Formula re-ranged: Looking for  $t$   $2.5\% = 0.025$

$$I = Prt$$
$$500 = 2000(2.5\%)t$$
$$\frac{500}{2000(2.5\%)}$$

$$\frac{500}{50} = \frac{50t}{50}$$

$$10 = t$$

**Example 2**

Allison wants to invest \$2000.00. Her bank offers an investment option that earns **compound interest** at a rate of 1.75% per year, compounded annually.

- If she invests the money for 1 year, how much interest will Allison earn?
- If she invests the money for 2 years, how much money will Allison have at the end of the investment term?
- Would you use the method from part b) for calculating the total value if Allison decides to invest her money for 10 years? Why or why not?

(a)  $I = 2000(1.75\%)(1)$   
 $= 35$   
 Total = \$2035

(b)  $I = 2035(1.75\%)(1) = 35.61$   
 $2070.61(1.75\%)(1)$

b)

**INTEREST TABLE**

Interest period	Investment value at beginning of period (\$)	Interest earned (\$) ( $I = Prt$ )	Investment value at end of period (\$)
1	\$2000.00	$\$2000.00 \times 0.0175 \times 1 = \$35.00$	$\$2000.00 + \$35.00 = \$2035.00$
2	\$2035.00	$\$2035.00 \times 0.0175 \times 1 = \$35.61$	$\$2000.00 + \$35.00 + \$35.61 = \$2070.61$

Way too long of a method.....

**Example 2**

Allison wants to invest \$2000.00. Her bank offers an investment option that earns compound interest at a rate of 1.75% per year, compounded annually.

- If she invests the money for 1 year, how much interest will Allison earn?
- If she invests the money for 2 years, how much money will Allison have at the end of the investment term?
- Would you use the method from part b) for calculating the total value if Allison decides to invest her money for 10 years? Why or why not?

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

$P = \$2000$   $r = 1.75\% = 0.0175$   $n = 1$

A is the final value of the investment (principal plus interest). 10

P is the principal.

r is the annual interest rate expressed as a decimal.

n is the number of compounding periods in a year.

t is the term of the investment or loan in years.

interest:

$$A = \left( 1 + \frac{r}{n} \right)^{(n \cdot t)} \text{ Exponent}$$

$$A = \$2000 \left( 1 + \frac{0.0175}{1} \right)^{(1 \times 10)}$$

$$A = \$2000 (1 + 0.0175)^{10}$$

$$A = 2000 (1.0175)^{10}$$

$$A = 2000 (1.189)$$

$$A = \$2378.89$$

B  
E  
D  
M  
A  
S

$$y^x = x^y$$

$$2^3 = 2 \cdot 2 \cdot 2$$

$$2^3 = 2^3$$

## Compound Interest Worksheets

Name \_\_\_\_\_

Calculate the total amount of the investment or total paid in a loan in the following situations:

1.) You invested \$52,400 at 6% compounded annually for 5 years. What is your total return on this investment?

Answer: \$70,123.02

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$
$$A = (52\,400) \left( 1 + \frac{0.06}{1} \right)^{(1 \times 5)}$$
$$P = 52\,400$$
$$r = 6\% = 0.06$$
$$n = 1$$
$$t = 5$$



1.) You invested \$52,400 at 6% compounded annually for 5 years. What is your total return on this investment?

Answer:

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

$$A = 52,400 \left( 1 + \frac{0.06}{1} \right)^{(1)(5)}$$

$$A = \$70,123.02$$

2.) You borrowed \$10,400 for 4 years at 12.7% and the interest is compounded semi-annually. What is the total you will pay back?

Answer: \$17,018.97

$$2) n = 2$$

$$A = 10,400 \left( 1 + \frac{0.127}{2} \right)^{2 \times 4}$$

$$A = 10,400 (1.0635)^8$$

$$A = \$17,018.97$$

3.) Your 2 year investment of \$5,300 earns 2.9% and is compounded annually. What will your total return be?

Answer: \$5,611.86

4.) You invested \$100 at 8.2% which is compounded annually for 7 years. How much will your \$100. be worth in 7 years?

Answer: \$173.62

5.) Your investment of \$18,100 at 13.6% compounded quarterly for  $7\frac{1}{2}$  years will be worth how much?

Answer: \$49,350.86