

# Chapter 3

## Length, Area, and Volume



*Kristi Hansen is a Red Seal plumber. Calculating the capacity of water lines, determining the length of pipe needed for drainage systems, and accurately predicting the volume of hot water a building's system will use are some of her tasks.*

### 3.1

#### Systems of Measurement

##### REVIEW: WORKING WITH PERIMETER

**perimeter:** the sum of the lengths of all the sides of a polygon

In this section, you will calculate the **perimeter** of different shapes.

A square is a quadrilateral with 4 equal sides, so the perimeter can be found by the following formula:

$$P = 4 \times (\text{side length})$$

The perimeter of a rectangle with length  $\ell$  and width  $w$  can be found by the following formula:

$$P = 2\ell + 2w$$

$$P = 2(\ell + w)$$

## Overview of Unit on Measurement

- SI system (metric system)
- Imperial system
- Converting within and between
- Measuring
- Calculating lengths, volumes, areas, perimeters, surface areas, mass, temperatures in both systems
- 2-D & 3-D shapes

## Metric system intro.

 <http://www.youtube.com/watch?v=MekxJse2vgs>

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**Système International (SI)**- the metric system.

- basic unit of length is the metre

**Imperial System**- until 1970s it was the measuring system in Canada.

- system used in the United States.

- basic unit of length is the foot.

### Converting Between SI units

Conversions between units, is a skill needed when working with the metric system. The following example should be your primary way of converting units.

*Example: convert 152 meters in centimeters.*

*Solution:*

the value you are converting →  $\frac{152\cancel{m}}{1} \times \frac{100\text{ cm}}{1\cancel{\text{ meter}}} = 15,200\text{cm}$

this fraction is an equivalency that features the unit you are converting from as the denominator - and your target unit as the numerator

this is the answer obtained by canceling the meter units - leaving centimeters - which was your target unit

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**Practice converting** – show all your working which means using the conversion factor and units!!!!

1. 130 cm to m

$$130 \cancel{\text{cm}} \times \frac{1 \text{ m}}{100 \cancel{\text{cm}}} = 1.3 \text{ m}$$

2. 96.3 cm to m

$$96.3 \cancel{\text{cm}} \times \frac{1 \text{ m}}{100 \cancel{\text{cm}}} = 0.963 \text{ m}$$

3. 3.25 km to cm

$$3.25 \cancel{\text{km}} \times \frac{1000 \cancel{\text{m}}}{1 \cancel{\text{km}}} \times \frac{100 \cancel{\text{cm}}}{1 \cancel{\text{m}}} = 325000 \text{ cm}$$

### GMF 10 – Imperial System

In Canada we use both the metric and imperial system. The imperial system is used in many trades like plumbing and carpentry. The imperial system is not a decimal system. Each group of units has a particular relationship.

#### Units for length:

|                         |           |           |            |  |
|-------------------------|-----------|-----------|------------|--|
| <b>1 inch (in or ")</b> |           |           |            |  |
| <b>1 foot (ft or ')</b> | 12 inches |           |            |  |
| <b>1 yard (yd)</b>      | 36 inches | 3 feet    |            |  |
| <b>1 mile (mi)</b>      |           | 5280 feet | 1760 yards |  |

GMF 10

Graham

**Practice converting** – show all your working which means using the conversion factor and units!!!!

1. 41 inches to cm

$$41'' \times \frac{2.54 \text{ cm}}{1''} = 104.14 \text{ cm}$$

2.  $5\frac{1}{2}$  yds to inches

$$5\frac{1}{2} \text{ yd} \times \frac{36''}{1 \text{ yd}} = 198 \text{ inches}$$

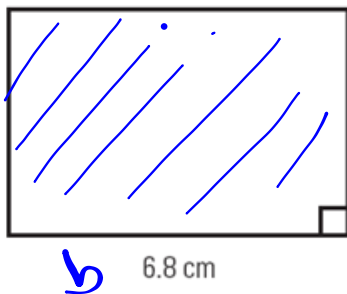
3. 6 ft to yards

$$6 \text{ ft} \times \frac{1 \text{ yd}}{3 \text{ ft}} = 2 \text{ yds}$$

Examples

Calculate the area of each figure:

(a)

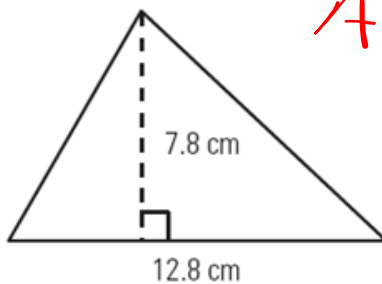


$$A = 6.8 \times 4.5$$

$$h \quad A = 30.6 \text{ cm}^2$$

$$30.6 \text{ cm}^2 \times \frac{1 \text{ in}^2}{(2.54 \text{ cm})^2}$$

(b)



$$\text{Area in cm}^2 = \underline{4.7} \text{ in}^2$$

$$A_T = \frac{b \times h}{2} = 49.92 \text{ cm}^2$$

$$49.92 \text{ cm}^2 \times \frac{1 \text{ in}^2}{(2.54 \text{ cm})^2}$$

$$\text{Area in cm}^2 = \underline{7.7} \text{ in}^2$$